

# Mathematics: analysis and approaches

## Formula booklet

SL & HL, first assessment 2021

Formulae grouped by topic.

**Provided in:** Papers 1, 2 and 3 (HL)

**Calculator:** Graphic display calculator (GDC), required in Papers 2 and 3. Not permitted in Paper 1.

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## Prior learning - SL and HL

|                                                                                            |                                                                                         |
|--------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------|
| Area of a parallelogram                                                                    | $A = bh$ , where $b$ is the base, $h$ is the height                                     |
| Area of a triangle                                                                         | $A = \frac{1}{2}(bh)$ , where $b$ is the base, $h$ is the height                        |
| Area of a trapezoid                                                                        | $A = \frac{1}{2}(a + b)h$ , where $a$ and $b$ are the parallel sides, $h$ is the height |
| Area of a circle                                                                           | $A = \pi r^2$ , where $r$ is the radius                                                 |
| Circumference of a circle                                                                  | $C = 2\pi r$ , where $r$ is the radius                                                  |
| Volume of a cuboid                                                                         | $V = lwh$ , where $l$ is the length, $w$ is the width, $h$ is the height                |
| Volume of a cylinder                                                                       | $V = \pi r^2 h$ ,<br>where $r$ is the radius, $h$ is the height                         |
| Volume of a prism                                                                          | $V = Ah$ , where $A$ is the area of cross-section, $h$ is the height                    |
| Area of the curved surface of a cylinder                                                   | $A = 2\pi rh$ ,<br>where $r$ is the radius, $h$ is the height                           |
| Distance between two points $(x_1, y_1)$ and $(x_2, y_2)$                                  | $d = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$                                              |
| Coordinates of the midpoint of a line segment with endpoints $(x_1, y_1)$ and $(x_2, y_2)$ | $\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$                                 |

# Topic 1: Number and Algebra - SL and HL

|        |                                                     |                                                                                                                                                                                                                                                            |
|--------|-----------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| SL 1.2 | The $n$ th term of an arithmetic sequence           | $u_n = u_1 + (n - 1)d$                                                                                                                                                                                                                                     |
|        | The sum of $n$ terms of an arithmetic sequence      | $S_n = \frac{n}{2} (2u_1 + (n - 1)d) ; S_n = \frac{n}{2} (u_1 + u_n)$                                                                                                                                                                                      |
| SL 1.3 | The $n$ th term of a geometric sequence             | $u_n = u_1 r^{n-1}$                                                                                                                                                                                                                                        |
|        | The sum of $n$ terms of a finite geometric sequence | $S_n = \frac{u_1(r^n - 1)}{r - 1} = \frac{u_1(1 - r^n)}{1 - r}, r \neq 1$                                                                                                                                                                                  |
| SL 1.4 | Compound interest                                   | $FV = PV \times \left(1 + \frac{r}{100k}\right)^{kn}$ ,<br>where $FV$ is the future value, $PV$ is the present value,<br>$n$ is the number of years, $k$ is the number<br>of compounding<br>periods per year, $r\%$ is the nominal annual rate of interest |
| SL 1.5 | Exponents and logarithms                            | $a^x = b \Leftrightarrow x = \log_a b$ ,<br>where $a > 0, b > 0, a \neq 1$                                                                                                                                                                                 |
| SL 1.7 | Exponents and logarithms                            | $\log_a xy = \log_a x + \log_a y$<br>$\log_a \frac{x}{y} = \log_a x - \log_a y$<br>$\log_a x^m = m \log_a x$<br>$\log_a x = \frac{\log_b x}{\log_b a}$                                                                                                     |
| SL 1.8 | The sum of an infinite geometric sequence           | $S_\infty = \frac{u_1}{1 - r}, \ r\  < 1$                                                                                                                                                                                                                  |
| SL 1.9 | Binomial theorem,<br>$n \in \mathbb{N}$             | $(a + b)^n = a^n + \binom{n}{1} a^{n-1} b + \dots + \binom{n}{r} a^{n-r} b^r + \dots + b^n$<br>$\binom{n}{r} = \frac{n!}{r!(n-r)!}$                                                                                                                        |

## Topic 1: Number and Algebra - HL only

|          |                                                       |                                                                                                                                 |
|----------|-------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------|
| AHL 1.10 | Combinations<br>Permutations                          | $\binom{n}{r} = \frac{n!}{r!(n-r)!}$ $P(n, r) = \frac{n!}{(n-r)!}$                                                              |
| AHL 1.10 | Extension of binomial theorem, $n \in \mathbb{Q}$     | $(a + b)^n = a^n \left( 1 + n \left( \frac{b}{a} \right) + \frac{n(n-1)}{2!} \left( \frac{b}{a} \right)^2 + \dots \right)$      |
| AHL 1.12 | Complex numbers                                       | $z = a + bi$                                                                                                                    |
| AHL 1.13 | Modulus-argument (polar) and exponential (Euler) form | $z = r(\cos \theta + i \sin \theta) = re^{i\theta}$ $= r \operatorname{cis} \theta$                                             |
| AHL 1.14 | De Moivre's theorem                                   | $[r(\cos \theta + i \sin \theta)]^n = r^n(\cos n\theta + i \sin n\theta)$ $= r^n e^{in\theta} = r^n \operatorname{cis} n\theta$ |

## Topic 2: Functions - SL and HL

|        |                                                       |                                                                                  |
|--------|-------------------------------------------------------|----------------------------------------------------------------------------------|
| SL 2.1 | Equations of a straight line                          | $y = mx + c; ax + by + d = 0; y - y_1 = m(x - x_1)$                              |
|        | Gradient formula                                      | $m = \frac{y_2 - y_1}{x_2 - x_1}$                                                |
| SL 2.6 | Axis of symmetry of the graph of a quadratic function | $f(x) = ax^2 + bx + c \Rightarrow$ axis of symmetry is $x = -\frac{b}{2a}$       |
| SL 2.7 | Solutions of a quadratic equation                     | $ax^2 + bx + c = 0 \Rightarrow x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}, a \neq 0$ |
|        | Discriminant                                          | $\Delta = b^2 - 4ac$                                                             |
| SL 2.9 | Exponential and logarithmic functions                 | $a^x = e^{x \ln a}; \log_a a^x = x = a^{\log_a x}$ where $a, x > 0, a \neq 1$    |

## Topic 2: Functions - HL only

|          |                                                                                             |                                                                     |
|----------|---------------------------------------------------------------------------------------------|---------------------------------------------------------------------|
| AHL 2.12 | Sum and product of the roots of polynomial equations of the form $\sum_{r=0}^n a_r x^r = 0$ | Sum is $\frac{-a_{n-1}}{a_n}$ ; product is $\frac{(-1)^n a_0}{a_n}$ |
|----------|---------------------------------------------------------------------------------------------|---------------------------------------------------------------------|

## Topic 3: Geometry and trigonometry - SL and HL

|        |                                                                                                      |                                                                                                    |
|--------|------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------|
| SL 3.1 | Distance between two points $(x_1, y_1, z_1)$ and $(x_2, y_2, z_2)$                                  | $d = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2 + (z_1 - z_2)^2}$                                         |
|        | Coordinates of the midpoint of a line segment with endpoints $(x_1, y_1, z_1)$ and $(x_2, y_2, z_2)$ | $\left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2}, \frac{z_1+z_2}{2}\right)$                             |
|        | Volume of a right-pyramid                                                                            | $V = \frac{1}{3}Ah$ ,<br>where $A$ is the area of the base, $h$ is the height                      |
|        | Volume of a right cone                                                                               | $V = \frac{1}{3}\pi r^2 h$ ,<br>where $r$ is the radius, $h$ is the height                         |
|        | Area of the curved surface of a cone                                                                 | $A = \pi r l$ ,<br>where $r$ is the radius, $l$ is the slant height                                |
|        | Volume of a sphere                                                                                   | $V = \frac{4}{3}\pi r^3$ , where $r$ is the radius                                                 |
|        | Surface area of a sphere                                                                             | $A = 4\pi r^2$ , where $r$ is the radius                                                           |
| SL 3.2 | Sine rule                                                                                            | $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$                                           |
|        | Cosine rule                                                                                          | $c^2 = a^2 + b^2 - 2ab \cos C$ ; $\cos C = \frac{a^2+b^2-c^2}{2ab}$                                |
|        | Area of a triangle                                                                                   | $A = \frac{1}{2}ab \sin C$                                                                         |
| SL 3.4 | Length of an arc                                                                                     | $l = r\theta$ ,<br>where $r$ is the radius, $\theta$ is the angle measured in radians              |
|        | Area of a sector                                                                                     | $A = \frac{1}{2}r^2\theta$ ,<br>where $r$ is the radius, $\theta$ is the angle measured in radians |

|        |                            |                                                                                                 |
|--------|----------------------------|-------------------------------------------------------------------------------------------------|
| SL 3.5 | Identity for $\tan \theta$ | $\tan \theta = \frac{\sin \theta}{\cos \theta}$                                                 |
| SL 3.6 | Pythagorean identity       | $\cos^2 \theta + \sin^2 \theta = 1$                                                             |
|        | Double angle identities    | $\sin 2\theta = 2 \sin \theta \cos \theta$                                                      |
|        |                            | $\cos 2\theta = \cos^2 \theta - \sin^2 \theta$<br>$= 2 \cos^2 \theta - 1 = 1 - 2 \sin^2 \theta$ |

### Topic 3: Geometry and trigonometry - HL only

|          |                                                               |                                                                                                                                                                                                                                       |
|----------|---------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| AHL 3.9  | Reciprocal trigonometric identities<br>Pythagorean identities | $\sec \theta = \frac{1}{\cos \theta}$<br>$\operatorname{cosec} \theta = \frac{1}{\sin \theta}$<br>$1 + \tan^2 \theta = \sec^2 \theta$<br>$1 + \cot^2 \theta = \operatorname{cosec}^2 \theta$                                          |
| AHL 3.10 | Compound angle identities<br>Double angle identity for $\tan$ | $\sin(A \pm B) = \sin A \cos B \pm \cos A \sin B$<br>$\cos(A \pm B) = \cos A \cos B \mp \sin A \sin B$<br>$\tan(A \pm B) = \frac{\tan A \pm \tan B}{1 \mp \tan A \tan B}$<br>$\tan 2\theta = \frac{2 \tan \theta}{1 - \tan^2 \theta}$ |
| AHL 3.12 | Magnitude of a vector                                         | $\ \mathbf{v}\  = \sqrt{v_1^2 + v_2^2 + v_3^2},$<br>where $\mathbf{v} = \begin{pmatrix} v_1 \\ v_2 \\ v_3 \end{pmatrix}$                                                                                                              |

|          |                                                                                                              |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            |
|----------|--------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| AHL 3.13 | Scalar product<br>Angle between two vectors                                                                  | $\mathbf{v} \cdot \mathbf{w} = v_1 w_1 + v_2 w_2 + v_3 w_3,$ $\text{where } \mathbf{v} = \begin{pmatrix} v_1 \\ v_2 \\ v_3 \end{pmatrix}, \mathbf{w} = \begin{pmatrix} w_1 \\ w_2 \\ w_3 \end{pmatrix}$ $\mathbf{v} \cdot \mathbf{w} = \ \mathbf{v}\  \ \mathbf{w}\  \cos \theta,$ $\text{where } \theta \text{ is the angle between } \mathbf{v} \text{ and } \mathbf{w}$ $\cos \theta = \frac{v_1 w_1 + v_2 w_2 + v_3 w_3}{\ \mathbf{v}\  \ \mathbf{w}\ }$                                                                                                                               |
| AHL 3.14 | Vector equation of a line<br>Parametric form of the equation of a line<br>Cartesian equations of a line      | $\mathbf{r} = \mathbf{a} + \lambda \mathbf{b}$ $x = x_0 + \lambda l, y = y_0 + \lambda m, z = z_0 + \lambda n$ $\frac{x-x_0}{l} = \frac{y-y_0}{m} = \frac{z-z_0}{n}$                                                                                                                                                                                                                                                                                                                                                                                                                       |
| AHL 3.16 | Vector product<br>Area of a parallelogram                                                                    | $\mathbf{v} \times \mathbf{w} = \begin{pmatrix} v_2 w_3 - v_3 w_2 \\ v_3 w_1 - v_1 w_3 \\ v_1 w_2 - v_2 w_1 \end{pmatrix},$ $\text{where } \mathbf{v} = \begin{pmatrix} v_1 \\ v_2 \\ v_3 \end{pmatrix}, \mathbf{w} = \begin{pmatrix} w_1 \\ w_2 \\ w_3 \end{pmatrix}$ $\ \mathbf{v} \times \mathbf{w}\  = \ \mathbf{v}\  \ \mathbf{w}\  \sin \theta,$ $\text{where } \theta \text{ is the angle between } \mathbf{v} \text{ and } \mathbf{w}$ $A = \ \mathbf{v} \times \mathbf{w}\  \text{ where } \mathbf{v} \text{ and } \mathbf{w} \text{ form two adjacent sides of a parallelogram}$ |
| AHL 3.17 | Vector equation of a plane<br>Equation of a plane (using the normal vector)<br>Cartesian equation of a plane | $\mathbf{r} = \mathbf{a} + \lambda \mathbf{b} + \mu \mathbf{c}$ $\mathbf{r} \cdot \mathbf{n} = \mathbf{a} \cdot \mathbf{n}$ $ax + by + cz = d$                                                                                                                                                                                                                                                                                                                                                                                                                                             |

## Topic 4: Statistics and probability - SL and HL

|         |                                                                                               |                                                                                                                                               |
|---------|-----------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------|
| SL 4.2  | Interquartile range                                                                           | $IQR = Q_3 - Q_1$                                                                                                                             |
| SL 4.3  | Mean, $\bar{x}$ , of a set of data                                                            | $\bar{x} = \frac{\sum_{i=1}^k f_i x_i}{n}$ ,<br>where $n = \sum_{i=1}^k f_i$                                                                  |
| SL 4.5  | Probability of an event $A$<br>Complementary events                                           | $P(A) = \frac{n(A)}{n(U)}$<br>$P(A) + P(A') = 1$                                                                                              |
| SL 4.6  | Combined events<br>Mutually exclusive events<br>Conditional probability<br>Independent events | $P(A \cup B) = P(A) + P(B) - P(A \cap B)$<br>$P(A \cup B) = P(A) + P(B)$<br>$P(A   B) = \frac{P(A \cap B)}{P(B)}$<br>$P(A \cap B) = P(A)P(B)$ |
| SL 4.7  | Expected value of a discrete random variable $X$                                              | $E(X) = \sum_{i=1}^k x_i P(X = x_i)$                                                                                                          |
| SL 4.8  | Binomial distribution $X \sim B(n, p)$<br>Mean<br>Variance                                    | $E(X) = np$<br>$Var(X) = np(1 - p)$                                                                                                           |
| SL 4.12 | Standardized normal variable                                                                  | $z = \frac{x - \mu}{\sigma}$                                                                                                                  |

## Topic 4: Statistics and probability - HL only

|          |                                                    |                                                                                                                                                  |
|----------|----------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------|
| AHL 4.13 | Bayes' theorem                                     | $P(B   A) = \frac{P(B)P(A B)}{P(B)P(A B) + P(B')P(A B')}$ $P(B_i   A) = \frac{P(B_i)P(A B_i)}{P(B_1)P(A B_1) + P(B_2)P(A B_2) + P(B_3)P(A B_3)}$ |
| AHL 4.14 | Variance $\sigma^2$                                | $\sigma^2 = \frac{\sum_{i=1}^k f_i(x_i - \mu)^2}{n} = \frac{\sum_{i=1}^k f_i x_i^2}{n} - \mu^2$                                                  |
|          | Standard deviation $\sigma$                        | $\sigma = \sqrt{\frac{\sum_{i=1}^k f_i(x_i - \mu)^2}{n}}$                                                                                        |
|          | Linear transformation of a single random variable  | $E(aX + b) = aE(X) + b$ $\text{Var}(aX + b) = a^2 \text{Var}(X)$                                                                                 |
|          | Expected value of a continuous random variable $X$ | $E(X) = \mu = \int_{-\infty}^{\infty} x f(x) dx$                                                                                                 |
|          | Variance                                           | $\text{Var}(X) = E[(X - \mu)^2] = E(X^2) - [E(X)]^2$                                                                                             |
|          | Variance of a discrete random variable $X$         | $\text{Var}(X) = \sum (x - \mu)^2 P(X = x) = \sum x^2 P(X = x) - \mu^2$                                                                          |
|          | Variance of a continuous random variable $X$       | $\text{Var}(X) = \int_{-\infty}^{\infty} (x - \mu)^2 f(x) dx = \int_{-\infty}^{\infty} x^2 f(x) dx - \mu^2$                                      |

## Topic 5: Calculus - SL and HL

|        |                                                                                            |                                                                                                                                   |
|--------|--------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------|
| SL 5.3 | Derivative of $x^n$                                                                        | $f(x) = x^n \Rightarrow f'(x) = nx^{n-1}$                                                                                         |
| SL 5.5 | Integral of $x^n$<br>Area between a curve $y = f(x)$ and the $x$ -axis, where $f(x) > 0$   | $\int x^n dx = \frac{x^{n+1}}{n+1} + C, n \neq -1$<br>$A = \int_a^b y dx$                                                         |
| SL 5.6 | Derivative of $\sin x$                                                                     | $f(x) = \sin x \Rightarrow f'(x) = \cos x$                                                                                        |
|        | Derivative of $\cos x$                                                                     | $f(x) = \cos x \Rightarrow f'(x) = -\sin x$                                                                                       |
|        | Derivative of $e^x$                                                                        | $f(x) = e^x \Rightarrow f'(x) = e^x$                                                                                              |
|        | Derivative of $\ln x$                                                                      | $f(x) = \ln x \Rightarrow f'(x) = \frac{1}{x}$                                                                                    |
|        | Chain rule                                                                                 | $y = g(u), \text{ where } u = f(x)$<br>$\Rightarrow \frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx}$                           |
|        | Product rule                                                                               | $y = uv \Rightarrow \frac{dy}{dx} = u \frac{dv}{dx} + v \frac{du}{dx}$                                                            |
|        | Quotient rule                                                                              | $y = \frac{u}{v} \Rightarrow \frac{dy}{dx} = \frac{v \frac{du}{dx} - u \frac{dv}{dx}}{v^2}$                                       |
| SL 5.9 | Acceleration<br>Distance travelled from $t_1$ to $t_2$<br>Displacement from $t_1$ to $t_2$ | $a = \frac{dv}{dt} = \frac{d^2s}{dt^2}$<br>distance = $\int_{t_1}^{t_2} \ v(t)\  dt$<br>displacement = $\int_{t_1}^{t_2} v(t) dt$ |

|         |                                                  |                                       |
|---------|--------------------------------------------------|---------------------------------------|
| SL 5.10 | Standard integrals                               | $\int \frac{1}{x} dx = \ln \ x\  + C$ |
|         |                                                  | $\int \sin x dx = -\cos x + C$        |
|         |                                                  | $\int \cos x dx = \sin x + C$         |
|         |                                                  | $\int e^x dx = e^x + C$               |
| SL 5.11 | Area of region enclosed by a curve and $x$ -axis | $A = \int_a^b \ y\  dx$               |

## Topic 5: Calculus - HL only

|          |                                            |                                                                                                              |
|----------|--------------------------------------------|--------------------------------------------------------------------------------------------------------------|
| AHL 5.12 | Derivative of $f(x)$ from first principles | $y = f(x) \Rightarrow \frac{dy}{dx} = f'(x) = \lim_{h \rightarrow 0} \left( \frac{f(x+h) - f(x)}{h} \right)$ |
| AHL 5.15 | Standard derivatives                       |                                                                                                              |
|          | $f(x) = \tan x$                            | $f'(x) = \sec^2 x$                                                                                           |
|          | $f(x) = \sec x$                            | $f'(x) = \sec x \tan x$                                                                                      |
|          | $f(x) = \operatorname{cosec} x$            | $f'(x) = -\operatorname{cosec} x \cot x$                                                                     |
|          | $f(x) = \cot x$                            | $f'(x) = -\operatorname{cosec}^2 x$                                                                          |
|          | $f(x) = a^x$                               | $f'(x) = a^x (\ln a)$                                                                                        |
|          | $f(x) = \log_a x$                          | $f'(x) = \frac{1}{x \ln a}$                                                                                  |
|          | $f(x) = \arcsin x$                         | $f'(x) = \frac{1}{\sqrt{1-x^2}}$                                                                             |
|          | $f(x) = \arccos x$                         | $f'(x) = -\frac{1}{\sqrt{1-x^2}}$                                                                            |
|          | $f(x) = \arctan x$                         | $f'(x) = \frac{1}{1+x^2}$                                                                                    |

|          |                                                                                                     |                                                                                                                                                                                                                                                                                 |
|----------|-----------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| AHL 5.15 | Standard integrals                                                                                  |                                                                                                                                                                                                                                                                                 |
|          | $\int a^x \, dx$                                                                                    | $\frac{1}{\ln a} a^x + C$                                                                                                                                                                                                                                                       |
|          | $\int \frac{1}{a^2 + x^2} \, dx$                                                                    | $\frac{1}{a} \arctan\left(\frac{x}{a}\right) + C$                                                                                                                                                                                                                               |
|          | $\int \frac{1}{\sqrt{a^2 - x^2}} \, dx$                                                             | $\arcsin\left(\frac{x}{a}\right) + C, \ x\  < a$                                                                                                                                                                                                                                |
| AHL 5.16 | Integration by parts                                                                                | $\int u \frac{dv}{dx} \, dx = uv - \int v \frac{du}{dx} \, dx$ or $\int u \, dv = uv - \int v \, du$                                                                                                                                                                            |
| AHL 5.17 | Area of region enclosed by a curve and $y$ -axis<br>Volume of revolution about the $x$ or $y$ -axes | $A = \int_a^b \ x\  \, dy$<br>$V = \int_a^b \pi y^2 \, dx$ or $V = \int_a^b \pi x^2 \, dy$                                                                                                                                                                                      |
| AHL 5.18 | Euler's method<br>Integrating factor for $y' + P(x)y = Q(x)$                                        | $y_{n+1} = y_n + h \times f(x_n, y_n); x_{n+1} = x_n + h,$<br>where $h$ is a constant (step length)<br>$e^{\int P(x) \, dx}$                                                                                                                                                    |
| AHL 5.19 | Maclaurin series                                                                                    | $f(x) = f(0) + x f'(0) + \frac{x^2}{2!} f''(0) + \dots$                                                                                                                                                                                                                         |
|          | Maclaurin series for special functions                                                              | $e^x = 1 + x + \frac{x^2}{2!} + \dots$<br>$\ln(1+x) = x - \frac{x^2}{2} + \frac{x^3}{3} - \dots$<br>$\sin x = x - \frac{x^3}{3!} + \frac{x^5}{5!} - \dots$<br>$\cos x = 1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \dots$<br>$\arctan x = x - \frac{x^3}{3} + \frac{x^5}{5} - \dots$ |